

# Overview of activities

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and  
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Institute of Thermomechanics of the CAS, Prague

September 6, 2022

- ▶ Prof. M. Okrouhlík
- ▶ Dr. Jiří Plešek
- ▶ Dr. Ján Kopačka
- ▶ Dr. Dušan Gabriel
- ▶ Dr. Alena Kruisová
- ▶ Dr. Jan Trnka
- ▶ Dr. Robert Cimrman
- ▶ Dr. Ladislav Musil
- ▶ Dr. Jiří Šonský
- ▶ Dr. Jan Gruber
- ▶ Prof. Eduard Rohan
- ▶ Prof. Tomáš Roubíček
- ▶ Ing. Michal Mračko (FS CVUT)
- ▶ Ing. Xavier Arnoult (VŠCHT)
- ▶ Ing. et Ing. Radim Dvořák (FD CVUT)
- ▶ Vojtěch Kotek (FD CVUT)
- ▶ Miroslav Kylar (FD CVUT)
- ▶ Jindřich Bouška (FS CVUT)
- ▶ Jakub Malínek (FS CVUT)
- ▶ Jakub Fink (FEL CVUT)

# International collaborations

- ▶ Prof. K.C. Park, (Colorado Uni at Boulder, US)
- ▶ Prof. Jose Gonzalez (Uni of Seville, Spain)
- ▶ Prof. Michel Arrigoni (ENSTA Bretagne, Brest, France)
- ▶ Dr. A. Berezovski (Tallinn University of Technology, Estonia)
- ▶ Prof. S. Sorokin (University of Aalborg, Denmark)
- ▶ Dr. A. Tkachuk (University of Stuttgart, Germany / Karlstad University, Sweden)
- ▶ Prof. A. Popp (Bundeswehr University Munich, Germany).
- ▶ Dr. M. Geiß (OHB System AG, Munchen, Germany)
- ▶ Prof. Jin-Gyun Kim (Kyung Hee University, Suwon, Korea)
- ▶ Prof. Hoon Huh (KAIST, Daejeon, Korea)
- ▶ Dr. Ruben Acevedo (Centro Tecnológico – Universidade Federal de Santa Catarina, Brasil)

# Introduction of the Laboratory of computational mechanics

- ▶ Numerical methods in thermomechanics, material models, dynamic plasticity model identification via Taylor test
- ▶ Impact-contact problems, domain decomposition techniques
- ▶ Surface treatment - plasma shock peening
- ▶ Isogeometric analysis and coupling with FEM (geometry preserving simulations)
- ▶ Shock and wave propagation in solids
- ▶ Metamaterials and band gap problems
- ▶ Experimental study on impact mechanics
- ▶ Smart materials and structures, soft robotics, electroactive materials.
- ▶ Consultations for industry and summer short courses on numerical methods

Important projects: ESA LISA (gravity waves), OHB System AG (3D printed structures in aerospace objects), GAČR, TAČR. Computations of seismic risk on Mochovce power station.

Patents: Brno University of Technology (3D printing)

# Governing equations for elastodynamic problem

Strong form:

$$\begin{aligned}\operatorname{div} \boldsymbol{\sigma} + \mathbf{b} &= \rho \ddot{\mathbf{u}} & \text{in } \Omega \times [t^0, T] \\ \mathbf{u} &= \hat{\mathbf{u}} & \text{on } \Gamma_D \times [t^0, T] \\ \mathbf{n} \cdot \boldsymbol{\sigma} &= \hat{\mathbf{t}} & \text{on } \Gamma_N \times [t^0, T] \\ \mathbf{u}(\mathbf{x}, t^0) &= \mathbf{u}_0(\mathbf{x}) & \text{for } \mathbf{x} \in \Omega \\ \dot{\mathbf{u}}(\mathbf{x}, t^0) &= \dot{\mathbf{u}}_0(\mathbf{x}) & \text{for } \mathbf{x} \in \Omega\end{aligned}$$

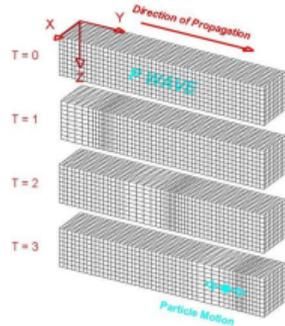
the Hooke's law and the infinitesimal strain tensor:

$$\boldsymbol{\sigma} = \mathbb{C} : \boldsymbol{\varepsilon}, \quad \boldsymbol{\varepsilon} = \frac{1}{2} \left[ (\operatorname{grad} \mathbf{u})^T + \operatorname{grad} \mathbf{u} \right]$$

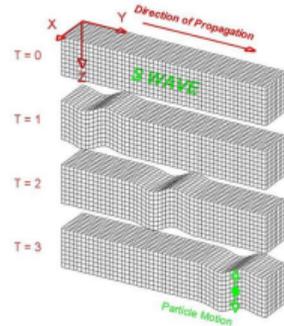
$u_i$  - the component of displacement vector  $\mathbf{u}(\mathbf{x}, t)$ ;  $\mathbf{x} \in \Omega$  - the position vector;  $\Omega$  - the domain of interest with the boundary  $\Gamma$ ;  $\sigma_{ij}$  - the Cauchy stress tensor (symmetric tensor);  $\varepsilon_{kl}$  - the infinitesimal strain tensor;  $\rho$  - mass density;  $b_i$  - the component of volume (body) intensity vector  $\mathbf{b}$ ;  $n_i$  - the component of the outward normal vector  $\mathbf{n}$  on  $\Gamma$ ;  $\hat{u}_i$  - the component of prescribed boundary displacement vector  $\mathbf{g}$ ;  $\hat{t}_i$  - the component of prescribed traction vector  $\mathbf{t}$ ;  $u_{0i}$  and  $\dot{u}_{0i}$  - the components of the initial displacement and velocity fields. **System of 15 linear hyperbolic PDEs.**

# Type of waves in continuum

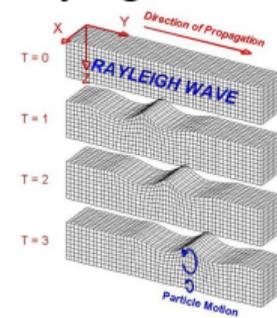
## P-wave



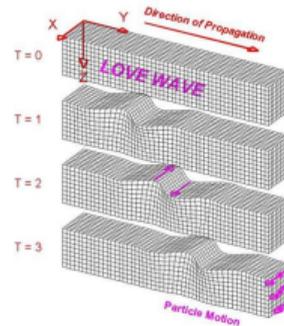
## S-wave



## Rayleigh's wave



## Love's wave



source: ©2007 Michigan Technological University;

<http://www.geo.mtu.edu/UPSeis/waves.html> **Other wave types:**

- ▶ waves in rods, flexural (bending) and torsional waves, guided waves
- ▶ Lamb's waves (waves in plates, dispersive, application in NDT)
- ▶ surface Rayleigh's waves (waves in a half-space)
- ▶ Love's waves (waves in a half-space covered by a layer with different elastic properties)
- ▶ von Schmidt's waves (reflected waves from boundaries)
- ▶ inter-facial Stoneley's (Leaky Rayleigh's) waves
- ▶ Scholte's waves (solid-liquid interface)

# Finite element method - recapitulation

Principle of virtual work in continuum mechanics:

$$\int_{\Omega} \delta \mathbf{u}^T \rho \ddot{\mathbf{u}} \, d\Omega + \int_{\Omega} \delta \boldsymbol{\varepsilon}^T \boldsymbol{\sigma} \, d\Omega = \int_{\Omega} \delta \mathbf{u}^T \mathbf{b} \, d\Omega + \int_{\Gamma_N} \delta \mathbf{u}^T \mathbf{t} \, d\Gamma$$

Using discretization of kinematic quantities we have

$$\delta \mathbf{q}^T \left[ \int_{\Omega} \rho \mathbf{N}^T \mathbf{N} \ddot{\mathbf{q}} \, d\Omega + \int_{\Omega} \mathbf{B}^T \boldsymbol{\sigma} \, d\Omega - \int_{\Omega} \mathbf{N}^T \mathbf{b} \, d\Omega - \int_{\Gamma_N} \mathbf{N}^T \mathbf{t} \, d\Gamma \right] = 0.$$

The previous equation should be valid for an arbitrary  $\delta \mathbf{q}$  respecting Dirichlet boundary conditions and, then the discretized equations of motion have the form

$$\mathbf{M} \ddot{\mathbf{q}} = \mathbf{f}^{ext} - \mathbf{f}^{int}$$

Other possibility is to use the Hamilton's principle of least action.

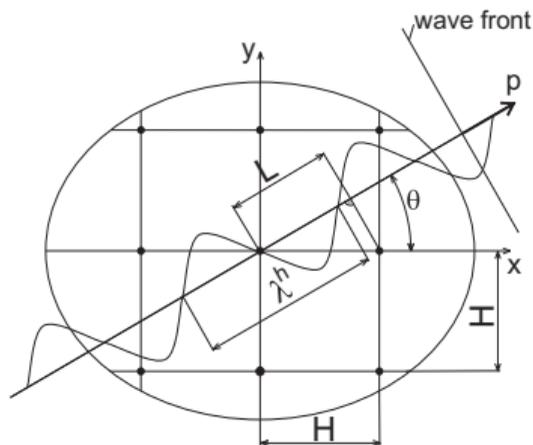
# Dispersion properties of finite element method

Characteristic equations of motion for patch

$$M_c \ddot{u}^h + K_c u^h = 0, \quad M = \int_V \rho H^T H dV, \quad K = \int_V B^T C B dV$$

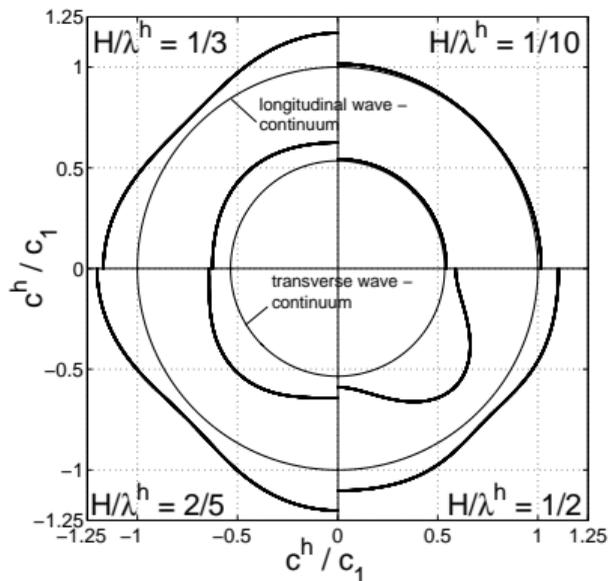
Fourier analysis - prescribed time nodal displacements

$$u_{mn}^h = U_{mn} \exp \left[ i \left( k^h x_m p_x + k^h y_n p_y - \omega t \right) \right]$$
$$v_{mn}^h = V_{mn} \exp \left[ i \left( k^h x_m p_x + k^h y_n p_y - \omega t \right) \right]$$

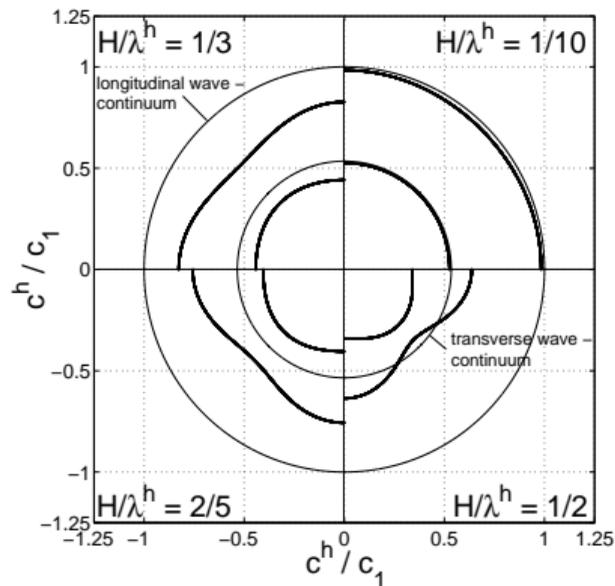


# Dispersion properties of finite element method

Consistent mass matrix



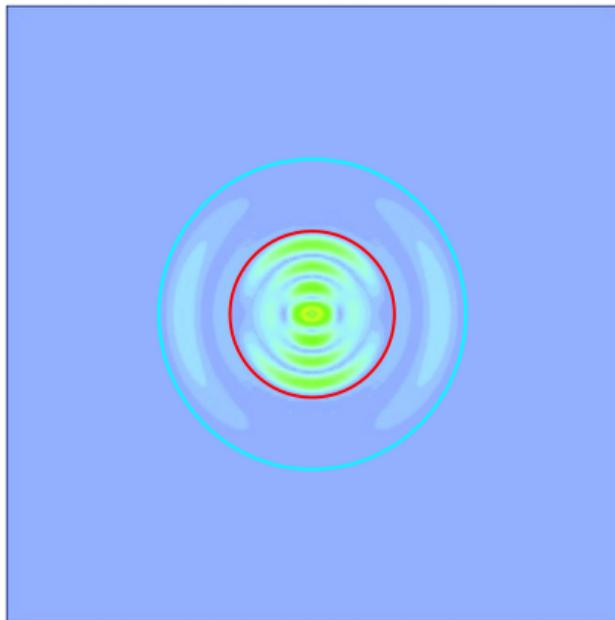
Lumped mass matrix



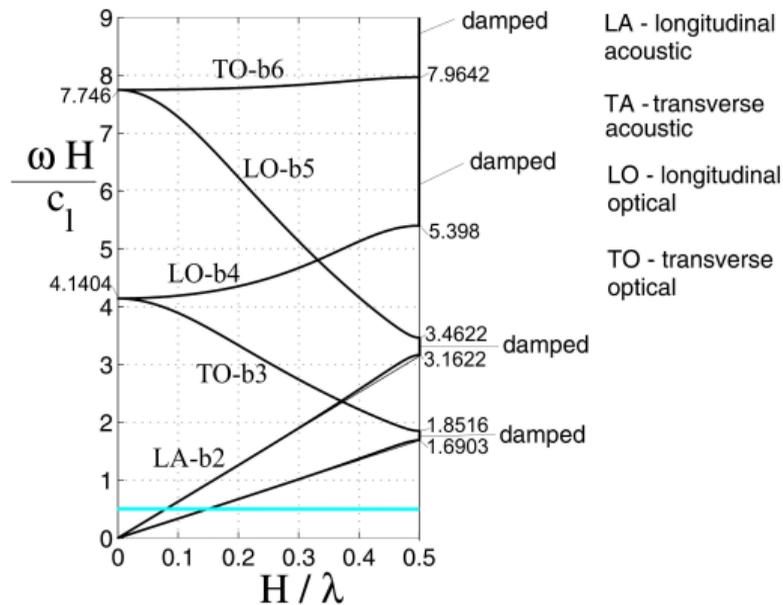
Anisotropic effect of FE discretization.

# Dispersion properties of finite element method

Wave field for frequency  $\omega H/c_1=0.5$

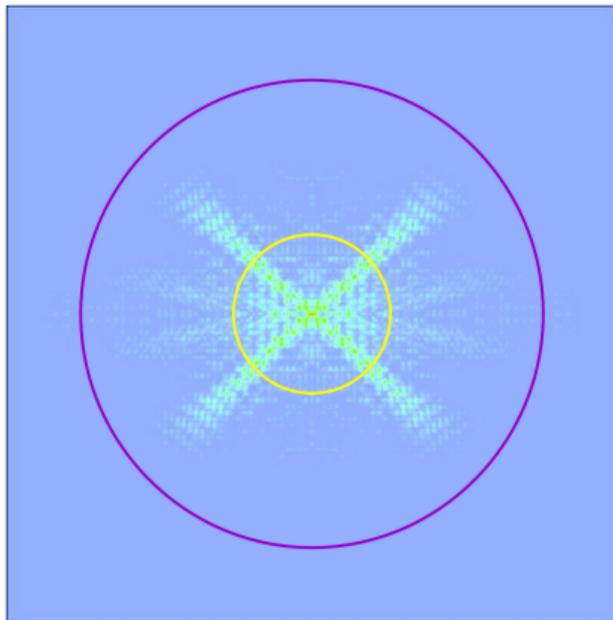


Dispersion spectrum

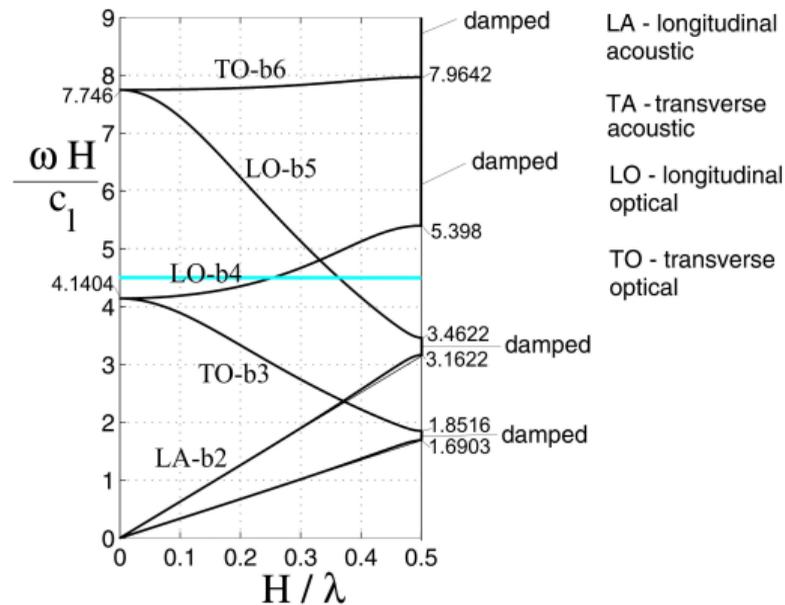


# Dispersion properties of finite element method

Wave field for frequency  $\omega H/c_1=4.5$



Dispersion spectrum



# Time stepping methods

the second-order system

$$\ddot{u} = f(u, \dot{u}, t) \text{ or } M\ddot{u}(t) + D\dot{u}(t) + Ku(t) = f^{ext}(t) - f^{contact}(t)$$

- ▶ The Newmark method
- ▶ The Houbolt method
- ▶ The Wilson  $\theta$  method
- ▶ The Midpoint method
- ▶ The Central difference method
- ▶ The HHT method
- ▶ The Generalized- $\alpha$  method
- ▶ Other methods

# Special time integration for spurious-stress-free oscillations

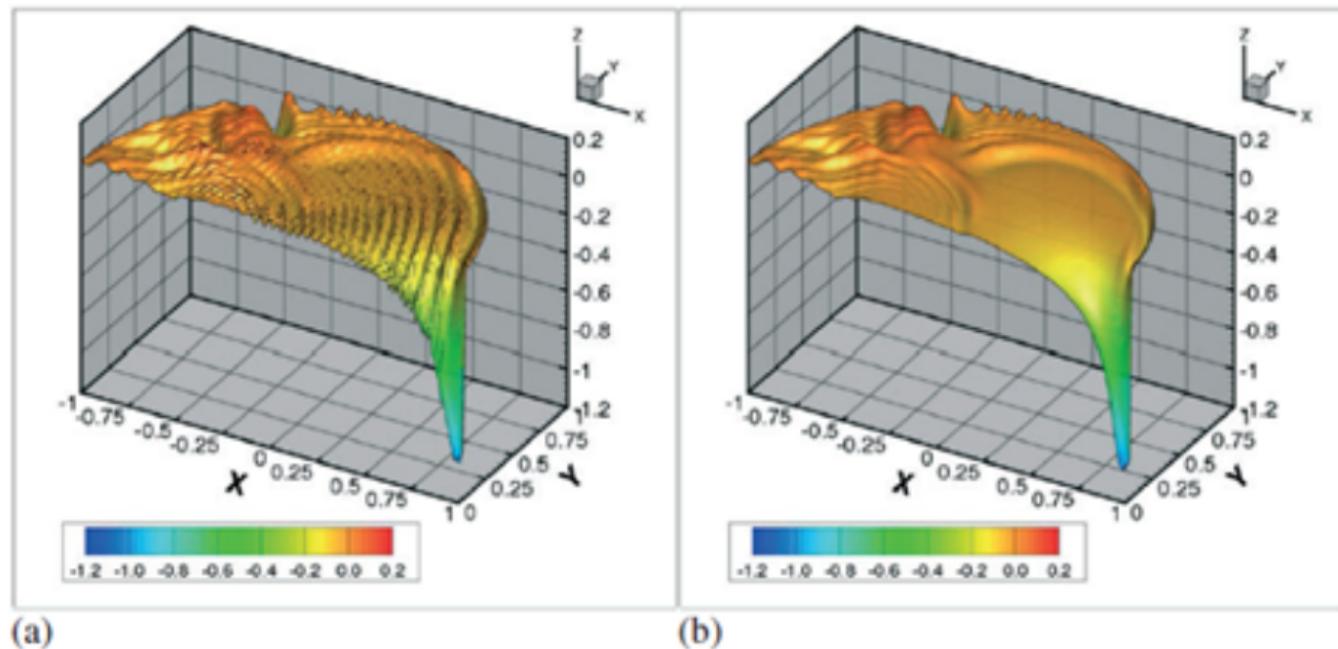
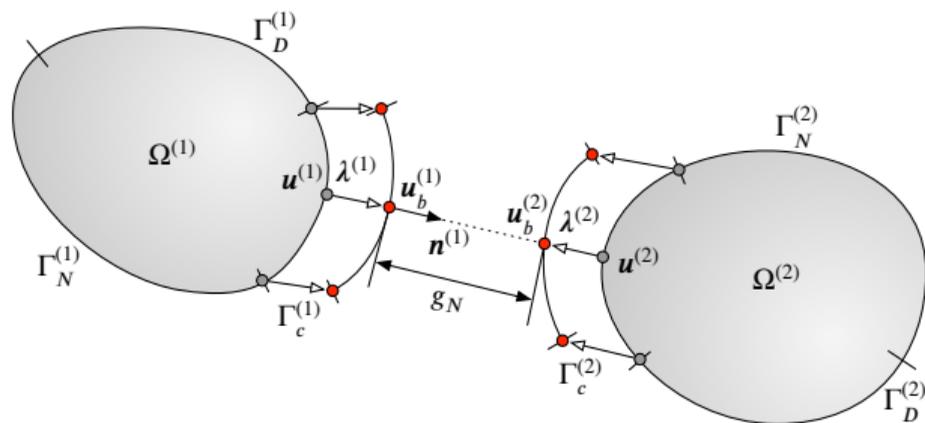


Figure 14. Distributions of dimensionless stress  $\sigma_{xx}/\sigma_0$  at the disc at the time  $4R/c_L$ : (a) the central difference method and (b) the proposed method. A half of a disc is shown.

# Partitioned formulation of contact-impact problems

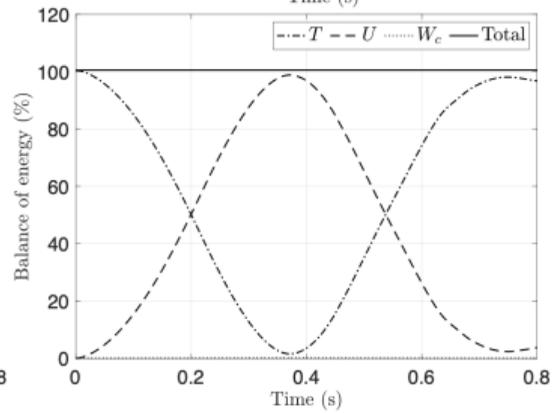
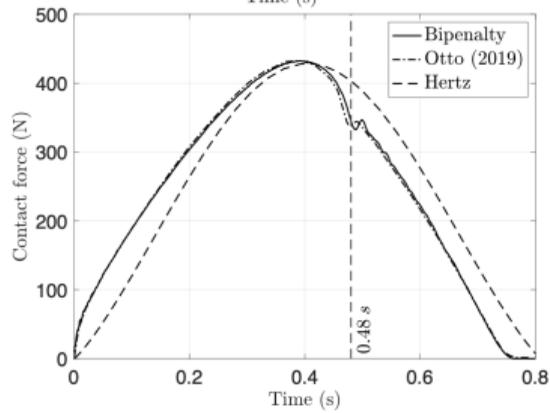
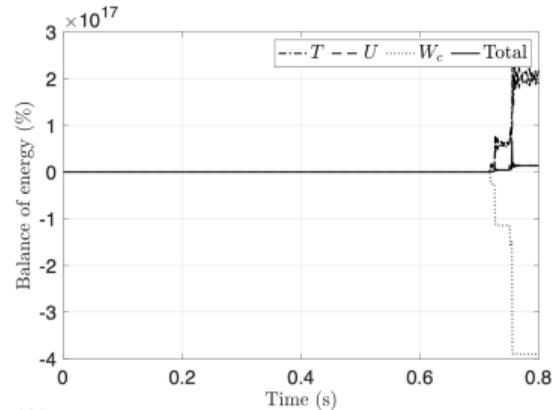
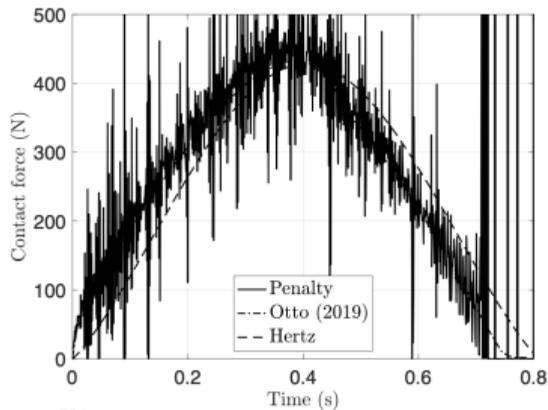


## Partitioned formulation of impact problems

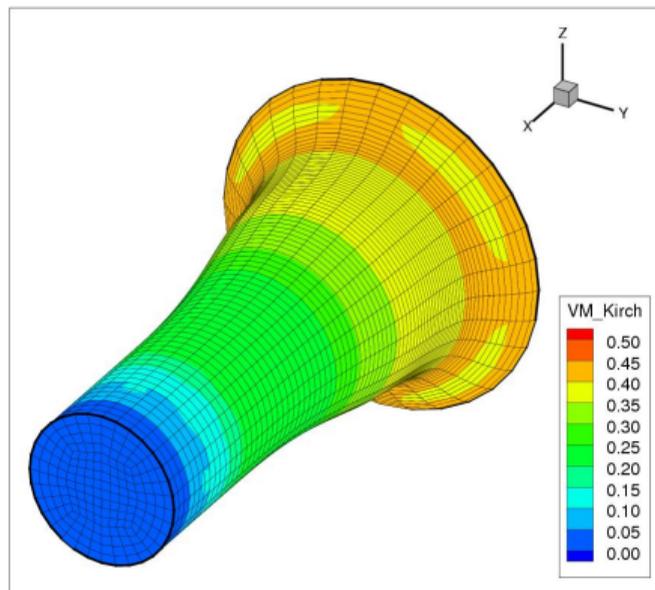
$$\begin{bmatrix} M & B & 0 \\ B^T & 0 & -L_c \\ 0 & -L_c^T & M_p \end{bmatrix} \begin{Bmatrix} \ddot{u} \\ \lambda \\ \ddot{u}_c \end{Bmatrix} = \begin{Bmatrix} r_u \\ 0 \\ -r_p \end{Bmatrix}$$

# Bi-penalty stabilized contact constraints

Comparison of the conventional penalty method and our proposed approaching



# Modelling of Taylor test



# Reciprocal mass matrices

Partitioned mixed formulation

$$A\dot{p} + B\lambda = r \quad \text{Equation of motion} \quad (1)$$

$$A^T\dot{u} - Cp = 0 \quad \text{Momentum equation} \quad (2)$$

$$B^T u - L_b u_b = 0 \quad \text{Boundary (and interface) constraints} \quad (3)$$

$$-L_b^T \lambda = 0 \quad \text{Newton's 3rd law on the boundaries} \quad (4)$$

Direct building of the inversion of mass matrix as

$$M^{-1} = A^{-T}CA^{-1} \quad (5)$$

# Mass scaling/tailoring

Modifying of the mass matrix so that the total mass is preserved and the higher frequency spectrum is improved.

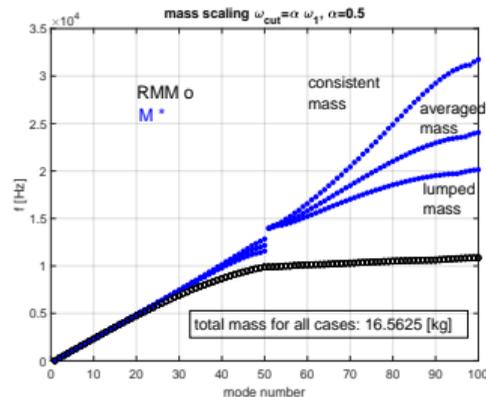
Mass scaled matrix:

$$M_{scaled} = M + \lambda \quad (6)$$

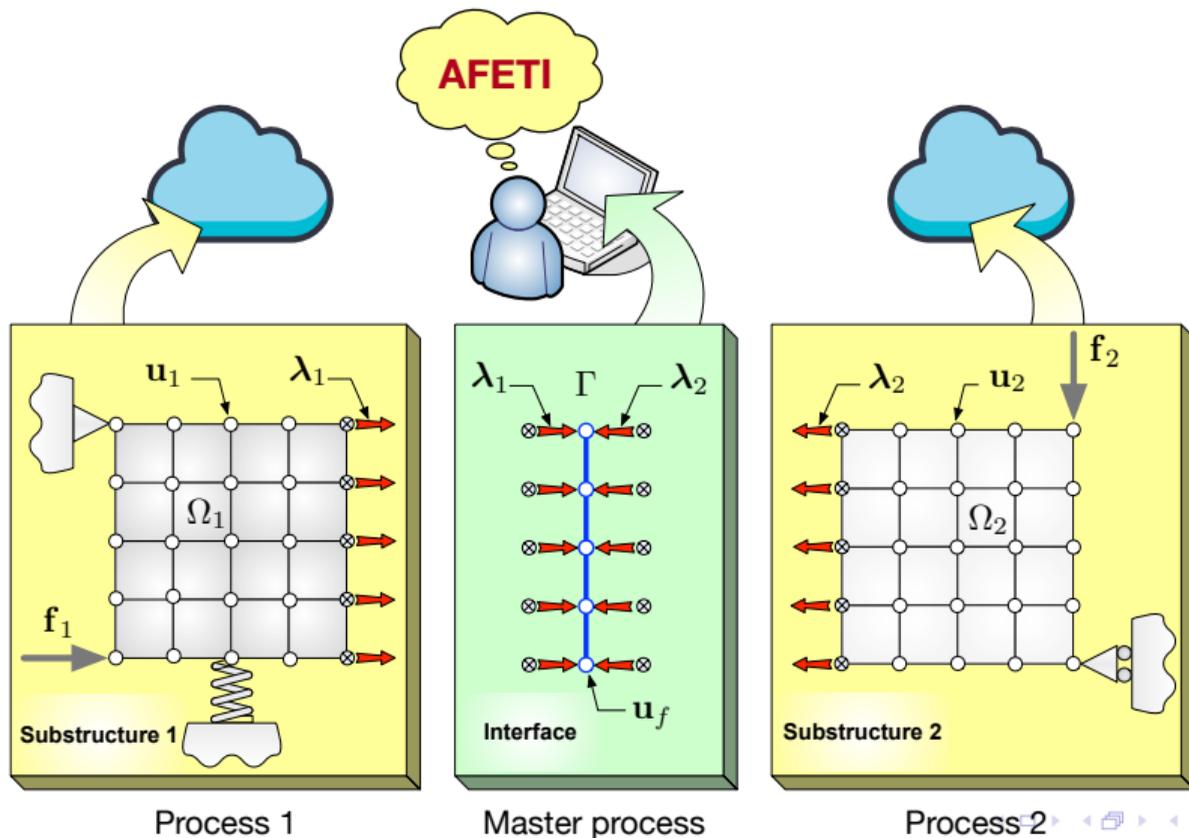
where

$$\lambda = M\Phi_h S \Phi_h^T M^T \quad (7)$$

where  $\Phi$  contents the higher mode shapes corresponding to eigen-modes for improving, S is the diagonal matrix with coefficients for cutting of value of higher eigen-frequencies.

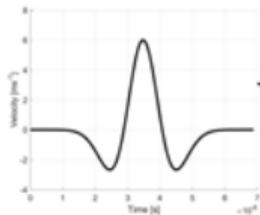


# Parallel computing: A-FETI solver including heterogeneous time integration (Radim Dvořák)

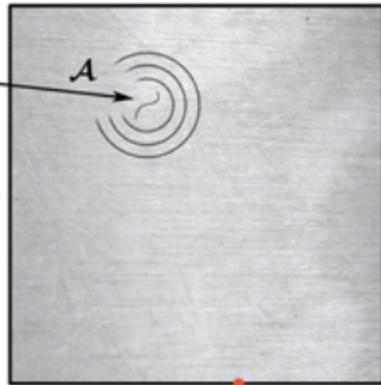


# Computational time reversal method for NDT applications

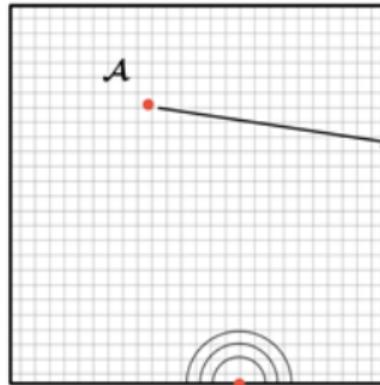
TIME HISTORY  
OF SOURCE



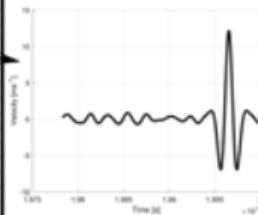
REAL PROBLEM/  
EXPERIMENT



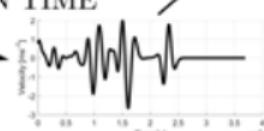
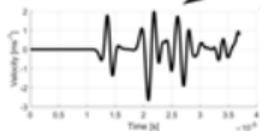
SIMULATION/  
COMPUTATION



RECONSTRUCTION OF TIME  
HISTORY OF SOURCE

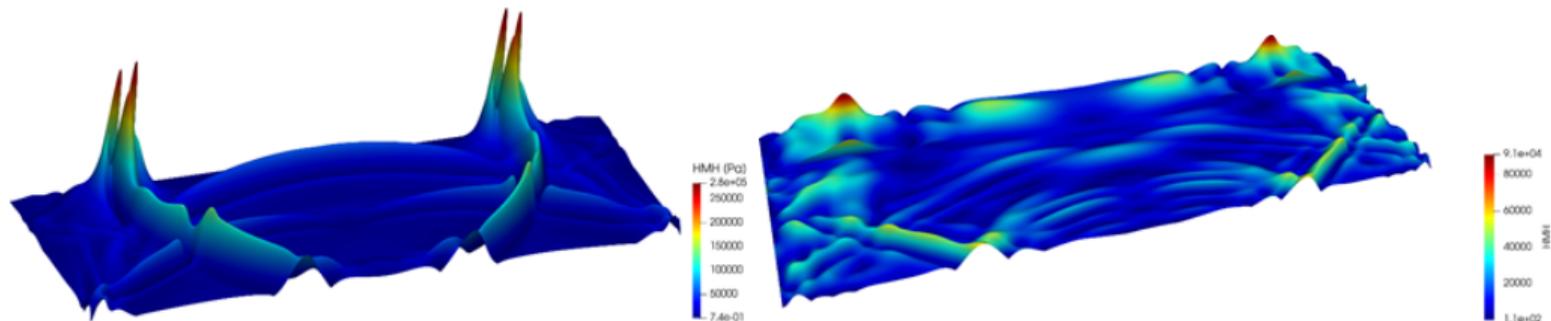


REVERSING IN TIME

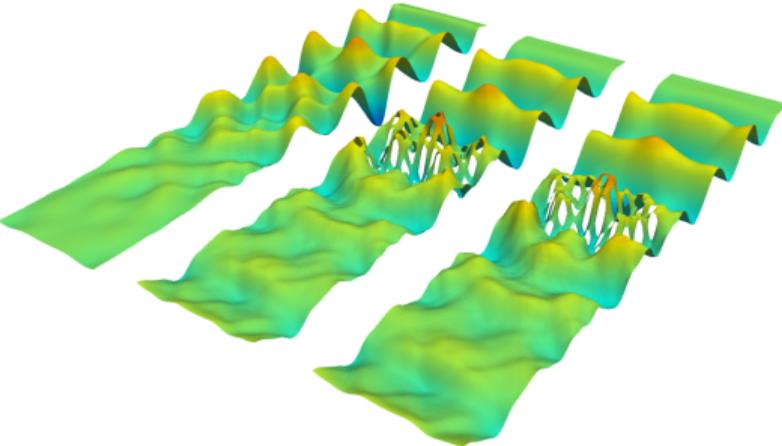
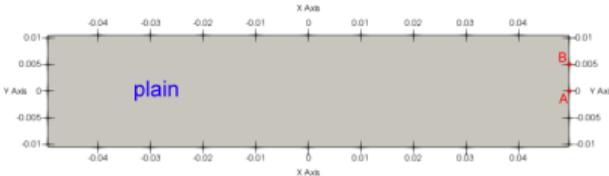


# Wave propagation in heterogeneous media

- ▶ 3D printed bimaterial problems
- ▶ Auxetic structures, Anisotropic media
- ▶ Space-time modulated materials
- ▶ Connection to topology optimization and material distributions



# Wave propagation in 3D printed structures (M. Mračko)



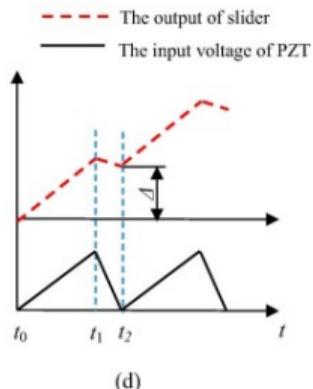
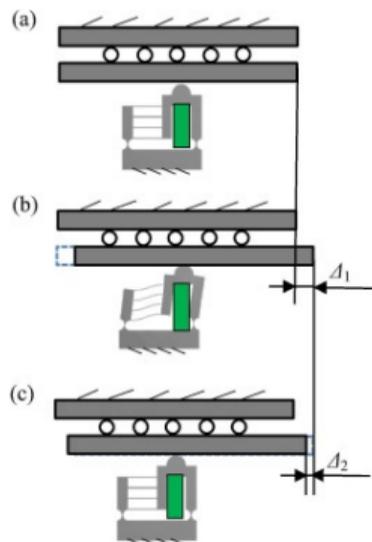
# Wave propagation in 3D printed auxetic structures



- Controllable metamaterials - GACR LA project 2022-2024 with Germany.
- Controlable metamaterials based on piezoelectric materials - Controllable gripping mechanics
- Shape morphing for fluid-structure interaction - Energy harvesting - Smart sensing events - Embedded sensors and actuators, adaptionic structures.

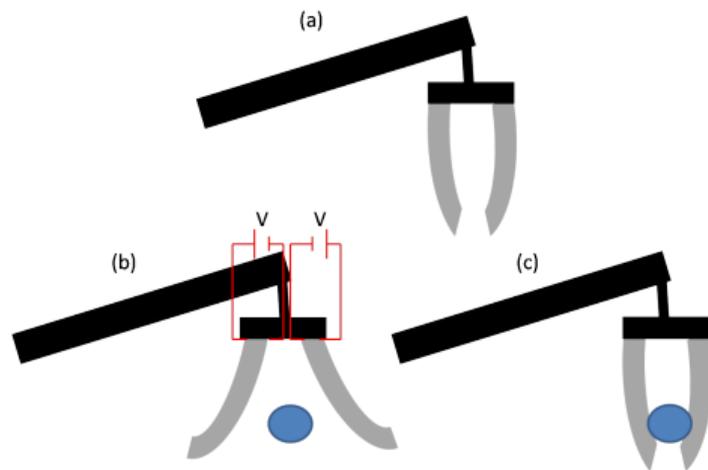
# Slip-stick mechanism for space applications

- ▶ piezoelectric actuators
- ▶ FSUA device for LISA ESA project - The Laser Interferometer Space Antenna. Launch is expected in 2037.



# Electro-active materials for controlable gripping

- ▶ electro-active polymers and gels
- ▶ piezoelectric materials including 3D printing technology
- ▶ flexoelectric materials

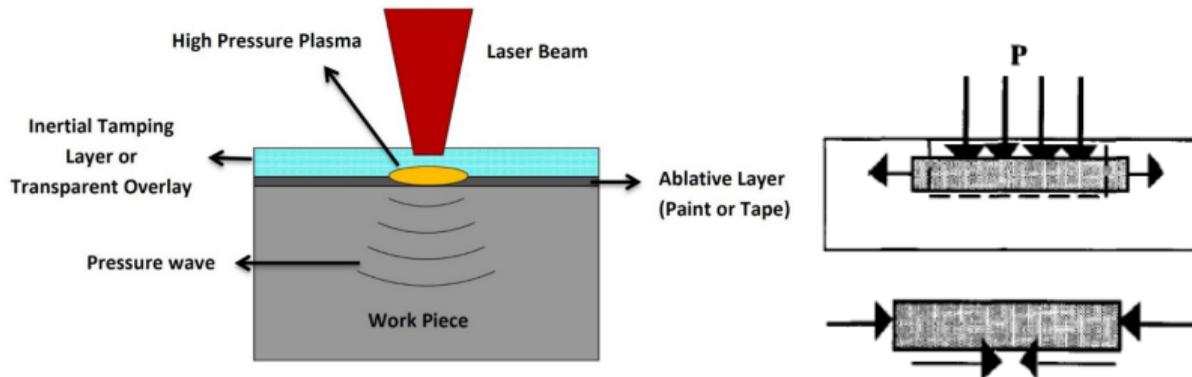


# Surface treatment

- ▶ Laser shock peening
- ▶ Plasma shock peening
- ▶ Plastic and shock waves, hardening
- ▶ Fatigue
- ▶ Corrosion resistance - collaboration with JRC
- ▶ Corrosion-Fatigue

# Principle of Laser Shock Peening

- ▶ The shock wave propagates to the target
- ▶ Causes plastic deformation to a depth at which the peak stress no longer exceeds the Hugoniot Elastic Limit (HEL) to the metal
- ▶ This plastic deformation generate Residual Stress Throughout the affected depth.

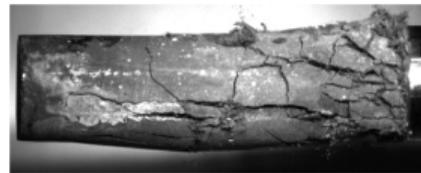
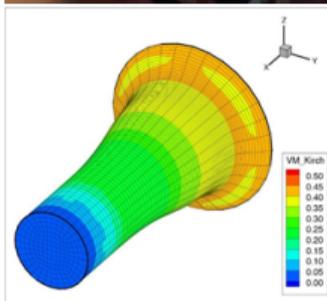


Now, we are working on Plasma shock peening technology under our patent.

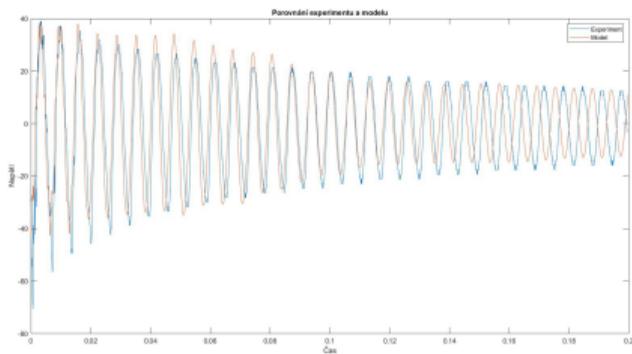
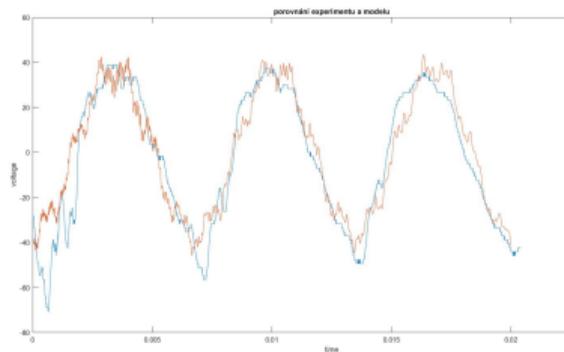
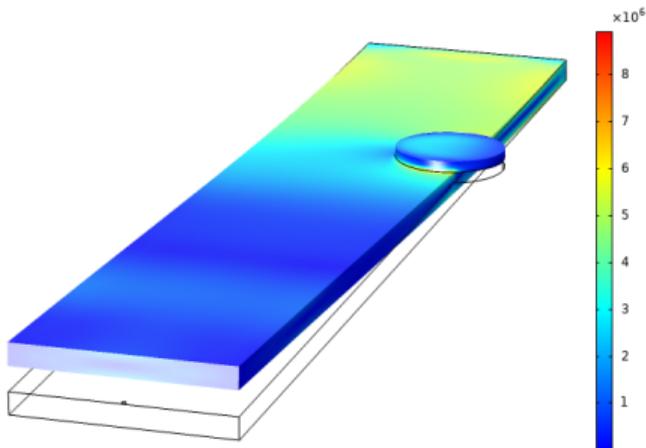
# Experiments in impact mechanics, wave propagation and vibration problems

## Experimental equipments:

- ▶ Taylor test wit air guns
- ▶ Split Hopkinson pressure bars
- ▶ Vibrometers



# Experiments in vibration problems with sensing by PZ materials



Thank you for your attention!!!